

$$\text{Q. 240) 2c) } v = \frac{2^t}{t}$$

$$\begin{aligned} v' &= \frac{\ln 2 \cdot 2^t \cdot t - 2^t \cdot (1)}{t^2} \\ &= \frac{2^t (t \ln 2 - 1)}{t^2} \end{aligned}$$

$$\text{d) } f(x) = \frac{\sqrt{3^x}}{x^2}$$

$$f'(x) = \frac{\frac{1}{2}(3^x)^{-\frac{1}{2}} \cdot 3^x \cdot \ln 3 \cdot x^2 - \sqrt{3^x} \cdot 2x}{x^4}$$

Unit 03: Lesson 1B – The Derivative of the Exponential Function

$$"e" = 2.718282\dots$$

$$\ln e = 1$$

ex: $y = e^{2x}$

$$y' = e^{2x} \cdot \boxed{\ln e} \cdot 2$$

$$= 2e^{2x}$$

ex: $y = x^2 \cdot e^{2x^2+x}$

$$y' = 2x \cdot e^{2x^2+x} + x^2 \cdot e^{2x^2+x} \cdot (4x+1)$$

ex: $y = 3x^3 \cdot \sqrt{4e^{2x}}$

$$y' = (9x^2)(4e^{2x})^{\frac{1}{2}} + (3x^3)\left(\frac{1}{2}\right) \cdot (4e^{2x})^{-\frac{1}{2}} \cdot \ln 4$$

$$\rightarrow (4e^{2x}) \cdot (e^{2x}) (\ln e) (2)$$

$$y = \frac{e^{2x^2} \cdot 3e^{2x}}{(\sqrt{e})^{3x}} \rightarrow (e^{\frac{1}{2}})^{3x} = e^{\frac{3}{2}x}$$

$$y' = \frac{[(e^{2x})(4x)(3e^{2x}) + (e^{4x})(3e^{2x})(\ln 3)(e^{2x})] (\sqrt{e})^{3x} - e^{\frac{3}{2}x} \cdot \left(\frac{3}{2}\right) \cdot (e^{2x^2} \cdot 3e^{2x})}{[(\sqrt{e})^{3x}]^2}$$